



**BAKER COLLEGE**  
**STUDENT LEARNING OUTCOMES**

**MTH4510 Introduction to Real Analysis**  
**3 Semester Hours**

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**Student Learning Outcomes & Enabling Objectives**

1. Generalize notions of limits, continuity, and derivatives.
  - a. Define limits, continuity, and derivatives.
  - b. Create examples to illustrate limits, continuity, and derivatives.
  - c. Determine limits, continuity, and derivatives of specific functions.
2. Validate proofs of limits using the epsilon-delta technique.
  - a. Construct proofs of the sum, product, quotient, and composition theorems for limits.
  - b. Construct a proof of the squeeze theorem.
  - c. Calculate specific examples using explicit epsilon and delta values.
  - d. Construct proofs involving different types of quantified statements.
3. Validate basic proofs of continuity for standard mathematical functions.
  - a. Construct proof of sum, product, quotient, and composition theorems for continuity.
  - b. Calculate specific examples using explicit epsilon and delta values.
4. Apply basic techniques of real analysis to theorems involving derivatives of functions.
  - a. Construct proofs of the general derivative theorems.
  - b. Construct proofs of derivatives for polynomial, rational, exponential, and logarithmic functions.
  - c. Compute specific examples using explicit limit computations.
5. Interpret derivatives in terms of optimization of functions.
  - a. Define maximum, minimum, and critical points.
  - b. Outline the main ideas required to complete the proofs of the Mean Value Theorem and Rolle's Theorem.
6. Generalize epsilon-delta techniques to functions of two variables.
  - a. Define an appropriate generalization of limit to functions of two variables.
  - b. Re-write basic theorems related to limits for functions of one variable to apply to functions of two variables.
  - c. Define an appropriate generalization of continuity to functions of two variables.
  - d. Re-write basic theorems related to continuity for functions of one variable to functions of two variables.
  - e. Demonstrate example epsilon-delta proof techniques for simple functions of two variables.

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## Big Ideas and Essential Questions

### Big Ideas:

- Limits and one-sided limits; when these exist.
- Continuity of a function on a set.
- The application of the epsilon-delta proof technique to limits and continuity.

### Essential Questions:

1. What is a limit? What is continuity? What is the relationship between the two?
2. What are the common strategies and “tricks” related to limits and epsilon-delta proofs?
3. How does the property of “continuity” factor into proofs about derivatives?
4. What is the formal definition of a derivative?

These SLOs are not approved for experiential credit.

**Effective: Fall 2017**